

Name:  
Period:  
Date

## Working with Sequences Using a Calculator Guided Notes

Press **Y=** and notice the difference in this screen.

To define a sequence, you must specify:

- $n\text{Min}$  - where you will start counting the numbers in the sequence (most likely this value is 1)
- $u(n)$  - the pattern for the sequence  
(use  $X, T, \theta, n$  key to enter the pattern)
- $u(n\text{Min})$  - the first number in the sequence  
(When you enter the first number in your sequence, notice the list braces that appear. These braces will allow for the entry of more than one term if needed.)

```
Plot1 Plot2 Plot3
nMin=1
u(n)=
u(nMin)=
v(n)=
v(nMin)=
w(n)=
w(nMin)=
```

## Working with Sequences

(in both **Seq** and **Func** Modes)

### In **Seq** MODE:

To work with sequences in the **Seq** mode:

- Press **MODE** key
- Choose **Seq** in the fourth line
- Hit **ENTER** to highlight **Seq**
- Leave other settings as default (on the left side)

```
Normal Sci Eng
Float 0123456789
Radian Degree
Func Par Pol Seq
Connected Dot
Sequential Simul
Real a+bi re^θi
Horiz G-T
```

**Example 1:** Consider the sequence defined as  $a_n = 2n - 1$ .

List the first 6 terms of the sequence and find the 105<sup>th</sup> term.

Enter the information in **Y=**:

```
Plot1 Plot2 Plot3
nMin=1
u(n)=2n-1
u(nMin)=1
v(n)=
v(nMin)=
w(n)=
w(nMin)=
```

Set the table (**TBLSET**):

```
TABLE SETUP
TblStart=1
ΔTbl=1
Indent: Auto Ask
Depend: Auto Ask
```

Look at the table (**TABLE**):

$n$	$u(n)$	
1	1	
2	3	
3	5	
4	7	
5	9	
6	11	
7	13	
$n=1$		

To find the 105<sup>th</sup> term, reset the **TblStart** to a value near (or at) the desired term.  
Read the answer from the table.

```
TABLE SETUP
TblStart=100
ΔTbl=1
Indent: AUTO Ask
Depend:  Ask
```

$n$	$u(n)$	
100	199	
101	201	
102	203	
103	205	
104	207	
105	209	
106	211	
$n=105$		

**Example 2:** (**Recursive sequence**) List the first 7 terms of the sequence:

$$a_1 = 3$$

$$a_n = \frac{2a_{n-1} - 1}{n}$$

Enter the recursive formula information.  
Enter the **u** by using the alpha letter **u**  
(2nd 7). Note the starting value of 3.

```
Plot1 Plot2 Plot3
nMin=1
u(n)=(2u(n-1)-1)/n
u(nMin)=(3)
u(n)=
u(nMin)=
u(n)=
```

View the terms of the sequence  
in the table.

$n$	$u(n)$	
1	3	
2	2.5	
3	1.3333	
4	.41667	
5	-.0333	
6	-.1778	
7	-.1937	
$n=1$		

**Example 3:** Generate the **Fibonacci Sequence** (where each term, after the first two terms, is determined by adding the two previous terms).

Enter the pattern for the sequence.  
Notice how the **u(nMin)** displays  
the first two terms using the  
list braces.

```
Plot1 Plot2 Plot3
nMin=1
u(n)=u(n-1)+u(n-2)
u(nMin)=(1,1)
u(n)=
u(nMin)=
u(n)=
```

Go to the table to view the  
Fibonacci sequence.

$n$	$u(n)$	
1	1	
2	1	
3	2	
4	3	
5	5	
6	8	
7	13	
$n=1$		

## In Func MODE:

Certain sequences can be examined in **Func** mode.  
Consider the following examples:

**Example 4:** Arithmetic and geometric sequences can be quickly generated in **Func** mode if the common difference or common ratio, respectively, are known, along with the starting value.

```
Sci Eng
Float 0123456789
Radian Degree
Func Par Pol Seq
Connected Dot
Sequential Simul
Real a+bi re^θi
Full Horiz G-T
```

List the first five terms of an arithmetic sequence whose first term is 1 and whose common difference is 4.

A "quick - see it on the screen" method:

- Enter the first term on the **home screen**.
- Press **ENTER** to register the first term.
- Press **+ 4** (the expression **Ans+4** will appear).
- Press **ENTER**.
- Continuing to press **ENTER** will generate successive terms in this sequence.

```
1
Ans+4
1
5
9
13
17
```

Unfortunately, finding specific terms with this method, such as the 100<sup>th</sup>, will require that you press **ENTER** and count very carefully - not always an easy process.

**Example 5:** If an expression/formula is known for the generation of a sequence, the terms can be listed in **Func** mode using the **seq()** function.

List the first 6 terms of the sequence defined by:  $a_n = \frac{1}{2^n}$

2nd **STAT (LIST)** → **OPS**  
Choose #5 **seq()**

```
NAMES OPS MATH
1:SortA(
2:SortD(
3:dim(
4:Fill(
5:seq(
6:cumSum(
7:List(
```

Using **seq()**, type the formula, variable, starting value for **n**, last value of **n** needed, increment. (For ease, **X** may be used as the variable -- or type **N** using the alpha key.) Arrow to the right to see more of the terms of the sequence.

If you need fractional answers, utilize the **MATH - #1 ► Frac**

```
seq(1/2^X,X,1,10
,1)
(.5 .25 .125 .0...
Ans►Frac
(1/2 1/4 1/8 1/...
```

This method of listing terms of a sequence will be **limited to 999 terms of the sequence** at any one time.

**Example 6:** If an expression/formula is known for the generation of a sequence, the sum of a specific number of terms can be found in **Func** mode.

Find the sum of the first 10 terms of the sequence defined by:  $a_n = 4n + 7$

2nd STAT (LIST) → MATH Notice that **sum** is followed by the entry of the sequence as shown in Example 5.  
Choose #5 **sum**(

```
NAMES OPS MATH
1:min(
2:max(
3:mean(
4:median(
5:sum(
6:Prod(
7:stdDev(
```

```
sum(seq(4X+7,X,
1,10,1))
290
```

Find the sum of the second through fifth terms of the sequence:  $a_n = 4n + 7$

```
sum(seq(4X+7,X,
2,5,1))
84
```

**Example 7:** Sequences represented by a recursive formula can be generated in **Func** mode.

List the first 4 terms of the sequence defined by:  $a_1 = 3$   
 $a_{n+1} = 2a_n - 1$

- Type the starting value and press **ENTER**.
- Use the **ANS** function to create the formula used to generate the sequence. Type **2\*ANS-1** and press **ENTER**.
- Now, simply press **ENTER** to create successive terms of the sequence.

```
3
2*Ans-1
3
5
7
9
11
13
```